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## The Study of a System Involving Equilibrium between Inner Sphere and Outer Sphere Complex Ions: $\text{Co}(\text{NH}_3)_5\text{H}_2\text{O}^{+++}$ and $\text{SO}_4^-$

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The fractional conversion of  $\text{Co}(\text{NH}_3)_5\text{H}_2\text{O}^{+++}$  to  $\text{Co}(\text{NH}_3)_5\text{SO}_4^+$  at equilibrium is observed to be almost independent of the concentration of sulfate ion over a wide range above *ca.* 0.01 *M*. The behavior is understood if the aquo ion is assumed to be converted to a sulfate complex ion by outer sphere association at low concentration of sulfate ion. The interpretation is confirmed by observations on the ultraviolet absorption band of  $\text{Co}(\text{NH}_3)_5\text{H}_2\text{O}^{+++}$  in the presence of varying amounts of sulfate ion. The change from the sulfato ion to the "isomeric" outer sphere complex ion is governed by the energy quantities:  $\Delta H = -4.0 \pm 0.3$  kcal. mole<sup>-1</sup>,  $\Delta S = -13$  cal. deg.<sup>-1</sup> mole<sup>-1</sup>. The reactions are first order in the concentration of  $\text{Co}(\text{III})$ . An increase in lability is observed with increase in sulfate ion concentration. The reactions are catalyzed by hydrogen ion. The activation energy for the change of the sulfato ion to the aquo ion is  $19.3 \pm 0.5$  and for the reverse change is  $23.7 \pm 0.5$  kcal. mole<sup>-1</sup>.

In considering the structure in solution of a complex ion the stoichiometry of which has been established, the question arises as to its distribution between two forms, in one of which the addend is directly attached to the central ion occupying a position in the first sphere of coordination, and in the other occupying a position outside the first sphere of coordination. The latter type of structure can be expected to have considerable stability when the central ion has a high charge and when the addend is an ion of high charge. The importance of association of this type in water solution has been proven by the work of Davies,<sup>1</sup> Linhard<sup>2</sup> and Katzenellenbogen<sup>3</sup> using complex cations of the type  $\text{Co}(\text{NH}_3)_6^{+++}$ . Replacement of  $\text{NH}_3$  by the anion does not take place under the conditions which were chosen and, in fact, the observations on the spectra<sup>2</sup> suggest that the first sphere of coordination is little disturbed in forming the outer sphere complex ions. It is evident that inert complex ions are extremely useful in defining the type of association under study, owing to the great difference in the speed at which association in the inner sphere and outer spheres takes place. For labile complex ions the distinction between the two types is much more difficult to make because the two forms are not readily separately characterized.

We have made use of an inert complex ion system also in our study. Substitution of water by water or other groups in  $\text{Co}(\text{NH}_3)_5\text{H}_2\text{O}^{+++}$  takes place very slowly.<sup>4</sup> Our data with this cation and with  $\text{SO}_4^-$  as an anion provide a dramatic demonstration of the presence in the solution of outer sphere complex ions, and furthermore, since  $\text{H}_2\text{O}$  and  $\text{SO}_4^-$  are eventually exchanged, have made possible a comparison of the stabilities of inner sphere and outer sphere "isomeric" forms. The desirability of a more complete study of this system was indicated by work done on the water exchange reaction.<sup>4</sup> The experiments we are reporting supplement those described by Adell.<sup>5</sup> His study was limited to the range of dilute solutions ( $(\text{SO}_4^-) \sim 10^{-2}$  or less) and therefore did not expose some of the interesting phenomena we have observed.

(1) C. W. Davies, *J. Chem. Soc.*, 2421 (1931).(2) M. Linhard, *Z. Elektrochem.*, **50**, 224 (1943).

(3) E. R. Katzenellenbogen, Paper No. 23, Division of Physical and Inorganic Chemistry, American Chemical Society Meeting, September, 1950.

(4) A. C. Rutenberg and H. Taube, *J. Chem. Phys.*, **20**, 823 (1952).(5) B. Adell, *Z. anorg. allgem. Chem.*, **246**, 303 (1942).

### Experimental

The procedure was to follow the extinction of a solution containing initially the ion  $\text{Co}(\text{NH}_3)_5\text{SO}_4^+$  or  $\text{Co}(\text{NH}_3)_5\text{H}_2\text{O}^{+++}$  in an environment of known composition as a function of time. In all cases equilibrium was approached from both sides, and in every case the final values of the extinction agreed to within 1%. For numerous solutions the rate was followed as a function of time starting for a given environment both with the sulfato and the aquo ion. In every case tested the specific rates *k* (defined as below), forward and reverse, agreed to within 3% if only total sulfate were present in sufficient excess. The values of the initial optical densities for the sulfato and aquo forms, and of the final optical density make possible the calculation of the equilibrium quotient, and these data, together with the specific rate for approach to equilibrium, lead to the specific rate of aquotization and sulfato formation for each solution. The optical densities were measured using a Beckman spectrophotometer. The wave length 560  $\mu$  at which the extinctions were measured lies on the long wave length side of a band with a maximum at 515  $\mu$  for the sulfato and 495 for the aquo ion. The two maxima in the visible for the ions are not sufficiently well separated to make them useful in analyzing the solution. While the strong ultraviolet band does differ markedly for the two substances, light of longer wave length was preferred since it permitted the use of Corex cells. The extinctions of  $\text{Co}(\text{NH}_3)_5\text{H}_2\text{O}^{+++}$  and  $\text{Co}(\text{NH}_3)_5\text{SO}_4^+$  at  $\lambda$  560  $\mu$  are changed somewhat (*cf.* Table I) as the environment changes, but only slightly as compared to the ultraviolet band. It was shown that the cobalt cations obey Beer's law in the solutions studied within experimental error. The extinctions change slightly with temperature—for example, there is an increase of *ca.* 3% in the extinction of the sulfato ion in 0.05 *M*  $\text{Na}_2\text{SO}_4$  as temperature rises from 25 to 31°—hence for a series all extinction measurements were made at constant ( $\pm 1^\circ$ ) temperature. In studying the variation of equilibrium constant with temperature the solutions which had been stored at different temperatures were all brought to the same temperature for comparison of optical densities. No significant readjustment in the inner sphere of coordination took place during the temperature change.

The substance  $[\text{Co}(\text{NH}_3)_5\text{SO}_4]\text{HSO}_4 \cdot 2\text{H}_2\text{O}$  was the source of the sulfato ion. It was prepared as described by Jorgensen.<sup>6</sup> The content of Co and  $\text{SO}_4$  were found to be 15.80% (theoretical, 15.79) and 51.42% (theoretical, 51.47).  $\text{Co}(\text{NH}_3)_5\text{H}_2\text{O}(\text{ClO}_4)_3$  was prepared as described elsewhere,<sup>4</sup> and served as the source of the aquo ion. The agreement of final optical densities starting with both salts shows that the aquo salt was a sufficiently good preparation. Other reagents were of A. R. quality, used without further purification. Solutions were made up using redistilled water.

**Conditions and Definitions.**—In all experiments except expt. 11, Table I, the concentration of sulfate was in excess of the concentration of the complex ion by a factor of 8 or greater. Over the greater part of the range investigated, the specific rate as well as the equilibrium distribution is not very sensitive to the concentration of  $\text{SO}_4^-$ , and the initial recorded values which differ at most by 7 or 8% from the equilibrium values, serve as sufficiently good de-

(6) S. M. Jorgensen, *J. prakt. Chem.*, [2] **31**, 268 (1885).

TABLE I  
DATA ON EQUILIBRIUM DISTRIBUTION AND RATE AS FUNCTION OF SULFATE CONCENTRATION  
Temperature  $31.1 \pm 0.02^\circ$ , except in expt. 8;  $\text{SO}_4^{2-}$  as  $\text{Na}_2\text{SO}_4$  except in expts. 5 and 6

No.	$\Sigma[\text{SO}_4^{2-}]$	$\Sigma[\text{H}^+]$	$k \times 10^4$	$D_0^S$	$D$	$D_0^A$	$Q_e$	$k_A \times 10^4$	$k_S \times 10^4$
1	2.90	0.30	11.3	0.491	0.328	0.213	1.42	6.6	4.7
2	1.15	.11	8.3	.495	.339	.214	1.25	4.6	3.7
3	0.57	.050	6.8	.501	.345	.213	1.18	3.7	3.1
4	.156	.015	4.8	.499	.345	.214	1.17	2.6	2.2
5	.156 <sup>a</sup>	.015	4.3	.499	.347	.214	1.14	2.3	2.0
6	.156 <sup>b</sup>	.015	5.2	.502	.348	.215	1.16	2.8	2.4
7	.052	.010	4.1	.506	.352	.214	1.12	2.2	1.9
8 <sup>c</sup>	.052	.010	17.0	.506	.371	.214	0.86	7.9	9.1
9	.021	.010	3.4	.508	.345	.217	1.28	1.9	1.5
10	.0140	.010	2.8	.510	.341	.217	1.36	1.7	1.2
11 <sup>d</sup>	.00216	.0061		.512	.321	.221	1.91		

<sup>a</sup>  $\text{K}_2\text{SO}_4$ . <sup>b</sup>  $\text{MgSO}_4$ . <sup>c</sup> Temperature  $43.8^\circ$ . <sup>d</sup>  $(\text{RSO}_4\text{HSO}_4) = 0.00108 M$ ;  $(\text{HClO}_4) = 0.005 M$ . No other electrolyte.

descriptions of the sulfate concentration prevailing. Except where otherwise recorded, sulfate was introduced as  $\text{Na}_2\text{SO}_4$ .

$\Sigma[\text{SO}_4^{2-}]$  refers to total  $\text{SO}_4^{2-}$  present, whether complexed or not (and differs but slightly from uncomplexed sulfate as noted above)

$\Sigma[\text{H}^+]$  represents concentration of  $\text{H}^+$  present in all forms

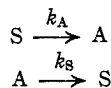
R represents the radical  $\text{Co}(\text{NH}_3)_5$

[A] represents the total concentration of species containing  $\text{RH}_2\text{O}^{+++}$

[S] represents the total concentration of species containing  $\text{RSO}_4^+$

$D_0^S$ ,  $D_0^A$  and  $D_\infty$  represent the optical densities ( $\log I_0/I$ ) of solutions containing S initially, A initially and the equilibrium mixture, respectively. For all solutions,  $cd = 0.0150 \text{ cm. mole l.}^{-1}$ .

$k$  is the specific rate of change as measured in a plot of  $\log |D_t - D_\infty|$  versus  $t$ . It is equal to the sum  $k_A + k_S$  where these specific rates refer to the processes



$Q_e$  represents the ratio  $[\text{A}]/[\text{S}]$  at equilibrium and is equal to  $k_A/k_S$ .

Specific rates are expressed with time in minutes.

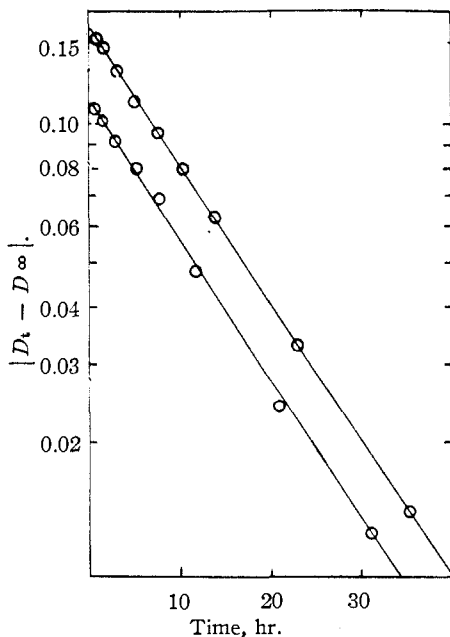


Fig. 1.—The variation of optical density with time medium,  $\Sigma[\text{SO}_4^{2-}] = 2.90 M$ ,  $\Sigma[\text{H}^+] = 0.3 M$ . Upper curve, sulfato salt approaching equilibrium; lower curve, roseo salt.  $D$  same for both.

## Results

In Fig. 1 are presented typical data on the change of optical density with time, starting in one experiment with the aquo salt and in another with the sulfato salt.

Table I contains a summary of results obtained at relatively low acidity with  $[\text{SO}_4^{2-}]$  as the principal concentration variable. Acid was present in all solutions to suppress the acid dissociation of  $\text{RH}_2\text{O}^{+++}$ . The results reported later show that  $(\text{H}^+)$  (or  $(\text{HSO}_4^-)$ ) is not an important variable at the levels used in the series in Table I.

Table II is a summary of the data obtained on the variation of  $Q_e$  with temperature. The data are shown plotted

TABLE II

VARIATION OF EQUILIBRIUM CONSTANT WITH TEMPERATURE

$\Sigma[\text{SO}_4^{2-}]$	Medium	$\Sigma[\text{H}^+]$	$Q_e$ at $24.9^\circ$	$Q_e$ at $31.1^\circ$	$Q_e$ at $43.8^\circ$
2.90		0.30	1.67	1.42	1.11
0.052		.010	1.28	1.12	0.86
0.021		.010	1.44	1.27	1.01

in Fig. 2 to yield values of  $\Delta H$  in kcal./mole which are as follows for the change:  $\text{S} \rightarrow \text{A}$ .

$$-4.1 \pm 0.3 \text{ at } 2.6 M \text{ SO}_4^{2-}$$

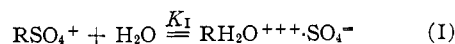
$$-4.0 \pm 0.3 \text{ at } 0.052 M \text{ SO}_4^{2-}$$

$$-3.6 \pm 0.3 \text{ at } 0.021 M \text{ SO}_4^{2-}$$

Table III presents data obtained for solutions containing also sodium perchlorate, Table IV for solutions with varying amounts of  $\text{NaHSO}_4$  and Table V for solutions with varying amounts of  $\text{NaHSO}_4$  and  $\text{H}_2\text{SO}_4$ . In Table VI some data dealing with the changes in extinction for the ultraviolet band of  $\text{RH}_2\text{O}^{+++}$  as  $\text{SO}_4^{2-}$  is added, are presented. The study of the spectra in solutions of various compositions is itself a major undertaking and more complete data for this and related systems will be presented in a future publication.

## Discussion

The most interesting feature of the equilibrium data is that the ratio  $Q_e$  is almost independent of  $(\text{SO}_4^{2-})$  over a wide concentration range, extending from 0.02 to 2.6  $M$ . It is further remarkable that this ratio instead of diminishing at high  $(\text{SO}_4^{2-})$ , in fact shows a slight increase in this concentration region. These observations suggest that the principal equilibrium operating over the range studied is



If ion pair formation is essentially complete even at 0.02  $M$   $\text{SO}_4^{2-}$  the change  $\text{S}$  to  $\text{A}$  involves species of the same stoichiometry with respect to  $\text{Co}(\text{III})$  and  $\text{SO}_4^{2-}$  and hence also of the same charge. Therefore the effects of salts, including  $\text{SO}_4^{2-}$ , is expected to be relatively slight. In the region of

TABLE III  
THE INFLUENCE OF NEUTRAL ELECTROLYTE

No.	$\Sigma[\text{SO}_4^-]$	$\Sigma[\text{H}^+]$	$(\text{NaClO}_4)$	Temperature 31.1°					
				$k \times 10^4$	$D_0^B$	$D_0^A$	$Q_e$	$k_A \times 10^4$	$k_S \times 10^4$
1	0.021	0.010	0.93	1.92	0.516	0.225	4.40	1.57	0.355
2 <sup>a</sup>	.054	.010	.71	2.56	.511	.223	2.13	1.74	0.82
3	.156	.010	.54	4.38	.506	.218	1.28	2.46	1.92
4	.054	.010	2.00	2.04	.524	.226	2.68	1.49	0.554
5	.156	.010	1.70	2.68	.507	.218	1.39	1.56	1.12

<sup>a</sup> The series was planned at constant  $\mu$ , but insufficient  $\text{NaClO}_4$  was inadvertently added in this experiment.

TABLE IV  
THE INFLUENCE OF BISULFATE ION

No.	$(\text{Na}_2\text{SO}_4)$	$(\text{NaHSO}_4)$	$(\text{NaClO}_4)$	Temperature 31.1°					
				$k \times 10^4$	$D_0^B$	$D_0^A$	$Q_e$	$k_A \times 10^4$	$k_S \times 10^4$
1	0.054	0.10	0.60	3.61	0.506	0.215	1.47	2.1	1.5
2	.054	.30	.40	4.62	.500	.215	1.35	2.6	2.0
3	.054	.70	.00	6.34	.499	.214	1.44	3.7	2.6
4	.54	.10	1.40	5.25	.503	.224	1.07	2.7	2.5
5	.54	.40	1.10	5.85	.500	.219	1.13	3.3	2.6
6	.54	1.50	0.00	9.02	.500	.214	1.42	5.4	3.6

TABLE V  
RATE AND EQUILIBRIUM DATA FOR SOLUTIONS CONTAINING  $\text{NaHSO}_4$  AND  $\text{H}_2\text{SO}_4$

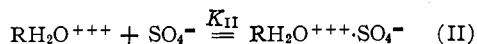
No.	$(\text{NaHSO}_4)$	$(\text{H}_2\text{SO}_4)$	Temperature 31.1°					
			$k \times 10^4$	$D_0^B$	$Q_e$	$k_A \times 10^4$	$k_S \times 10^4$	
1	0.00	3.00	16.1	0.488	2.87	11.9	4.2	
2	1.00	2.00	12.5	.496	2.14	8.5	4.0	
3	3.00	0.00	10.2	.496	1.61	6.3	3.9	
4	0.00	6.00	27.5	.485	2.26	19.1	8.4	
5	3.00	3.00	21.0	.488	1.94	13.9	7.1	
6	5.00	1.00	18.5	.490	1.69	11.6	6.9	
7	0.00	9.00	36.0	.460	1.40	21.	15.	

TABLE VI  
THE ULTRAVIOLET EXTINCTION COEFFICIENTS OF  $\text{Co}(\text{NH}_3)_5\text{H}_2\text{O}^{+++}$  AT VARIOUS CONCENTRATIONS OF SULFATE ION

Temperature  $27 \pm 1^\circ$ ;  $\epsilon = 1/cd \log I_0/I$  in  $l. \text{ mole}^{-1} \text{ cm}^{-1}$ ;  
 $(\text{RH}_2\text{O}(\text{ClO}_4)_3) = 8.0 \times 10^{-4} M$ ;  $(\text{HClO}_4) = 0.01 M$

$\lambda$ in $m\mu$	$\epsilon$ at $\Sigma(\text{SO}_4^-)$				
	0.000	0.0062	0.0125	0.0416	0.1040
270	15	26	34	42	44
260	31	76	89	112	118
250	143	257	288	338	360
245	336	503	538	613	650
240	762	990	1010	1120	1180
235	1620	1910	1940		

low sulfate ion concentration the equilibrium



presumably becomes important and  $\text{RH}_2\text{O}^{+++}$  as well as  $\text{RH}_2\text{O}^{+++}.\text{SO}_4^-$  contributes to [A]. At high concentration of  $\text{SO}_4^-$ ,  $Q_e$  will be altered by salt effects on equilibrium (I) or by further association of sulfate with the complex ions. However, the affinities of  $\text{RH}_2\text{O}^{+++}.\text{SO}_4^-$  and  $\text{RSO}_4^+$  for sulfate ion appear to be about the same, since  $Q_e$  changes only slightly even at high sulfate concentration.

The conclusion that  $\text{RH}_2\text{O}^{+++}$  and  $\text{SO}_4^-$  are strongly associated is supported by Davies' calculations<sup>1</sup> for the similar system  $\text{Co}(\text{NH}_3)_5^{+++}$  and  $\text{SO}_4^-$  which yielded  $3.3 \times 10^3$  as the equilibrium constant for the association reaction at

zero ionic strength and  $25^\circ$ . The conclusion is directly proven by the data in Table VI on the ultraviolet extinctions of  $\text{RH}_2\text{O}^{+++}$  in the presence of varying concentrations of  $\text{SO}_4^-$ . Marked changes in the extinction are observed in the ultraviolet band, with the extinctions at 240 and 235  $m\mu$  approaching saturation values when  $(\text{SO}_4^-)$  is only  $6 \times 10^{-3} M$ . More complete data will be required to obtain values of equilibrium con-

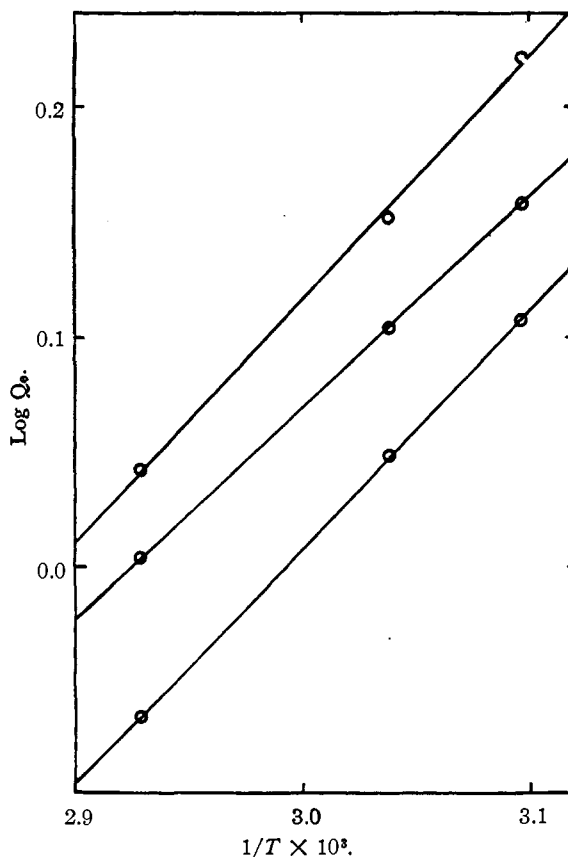


Fig. 2.—The variation of  $Q_e$  with temperature. Curves are in order for 2.90, 0.021 and 0.052  $M$ ,  $\Sigma[\text{SO}_4^-]$  reading from top to bottom.

stants, particularly because successive stages of association apparently must be taken into account. This is evidenced by the observation that the rate of approach to saturation extinction values is different at different wave lengths.

If the assumption is made that the ratio  $(\text{RH}_2\text{O}^{+++}\cdot\text{SO}_4^{=})/(\text{RSO}_4^+)$  remains constant below  $0.05 M \text{SO}_4^{=}$ , and is measured by the ratio  $Q_c$  at this sulfate ion concentration, the value of  $K_{11}$  for expt. 11 is calculated as  $1.1 \times 10^3$ . When corrected for the difference in  $\mu$ , this value will be close to that reported by Davies for  $\text{Co}(\text{NH}_3)_6^{+++}$  and  $\text{SO}_4^{=}$ .

The measured heats of reaction on the interpretation suggested apply to reaction I. It should be noted that the change is exothermic. It is interesting that the heat of transfer of  $\text{SO}_4^{=}$  from inner sphere to outer sphere does not change appreciably as  $(\text{SO}_4^{=})$  changes from  $0.05$  to  $2.6 M$ . The decrease in  $|\Delta H|$  at lower  $(\text{SO}_4^{=})$  can be attributed to participation by equilibrium (II). Using the observed values of equilibrium constant and  $\Delta H$  at  $0.05 M \text{SO}_4^{=}$ ,  $\Delta S$  at this concentration of sulfate is calculated as  $-13$  e.u. An entropy decrease can be expected since ions of opposite charge are separated in transferring  $\text{SO}_4^{=}$  from inner sphere to outer sphere, thus increasing the interaction with the solvent.

The effect of  $\text{NaClO}_4$  on the equilibrium  $[\text{A}]/[\text{S}]$  is presumably largely in increasing the concentration of  $\text{RH}_2\text{O}^{+++}$  relative to  $\text{RH}_2\text{O}^{+++}\cdot\text{SO}_4^{=} + \text{RSO}_4^+$ . There may also be an effect on the ratio  $(\text{RH}_2\text{O}^{+++}\cdot\text{SO}_4^{=})/(\text{RSO}_4^+)$ , but this is impossible to decide from the data. Assuming that the ratio is unaltered by  $\text{NaClO}_4$  and is given by the value of  $Q_c$  at  $0.05 M \text{SO}_4^{=}$ , the quotient  $K_{11}$  for expt. 1, Table III is calculated as 16, and for expt. 2 of the same table, at somewhat lower ionic strength as 20. The large change in  $K_{11}$  from the conditions of expt. 11 to those obtaining in the experiments of Table III, is in line with the large value of  $\Delta s^\ddagger$  for reaction (II).

The data of Table IV suggest that salts do affect the ratio  $(\text{RH}_2\text{O}^{+++}\cdot\text{SO}_4^{=})/(\text{RSO}_4^+)$ . While in dilute solution (expts. 1, 2, 3, Table IV)  $\text{NaClO}_4$  and  $\text{NaHSO}_4$  influence  $Q_c$  in approximately the same way, in more concentrated solution (expts. 4, 5, 6) replacing  $\text{NaClO}_4$  by  $\text{NaHSO}_4$  enhances the ratio. For concentrated electrolyte solutions effects due to changes in the activity of water must become important. The decrease in  $Q_c$  as the concentration of sulfuric acid is increased is attributable, in part at least, to this cause.

Over the composition range investigated, which includes variation of the initial concentration of  $\text{Co(III)}$  from  $0.0150$  to  $0.00150$  as well as the variation in concentrations of other ions, the reactions are first order in  $(\text{Co(III)})$ . Using solutions at lower  $(\text{SO}_4^{=})$  than we have in our rate study, Adell<sup>6</sup> observed  $k_A$  to be independent of  $\text{SO}_4^{=}$ , and  $k_S$  to be given by an expression of the form  $k^0 f(\text{SO}_4^{=}) (\text{RH}_2\text{O}^{+++})$ , where  $f$  is a function taking account of interionic attraction effects. For the conditions we have adopted,  $\text{RH}_2\text{O}^{+++}$  is almost completely associated with  $\text{SO}_4^{=}$ , so that the net change (except for further association of

$\text{Co(III)}$  and  $\text{SO}_4^{=}$ ) is represented in equation (I). The data of Table I exhibit the interesting feature that  $k_A$  and  $k_S$  are about equally affected by the concentration of sulfate ion for solutions in which  $\text{Co(III)}$  can be presumed to be almost completely associated with  $\text{SO}_4^{=}$ . The catalytic effect of sulfate ion is best demonstrated by observing its effect on  $k_A$  for solutions at constant ionic strength. Comparison of expts. 1, 2 and 3 of Table III shows that  $\text{SO}_4^{=}$  increases the rate of removal of  $\text{SO}_4^{=}$  from the inner coordination sphere. Catalysis by anions of substitution reactions in complex ions has been observed in other cases.<sup>7,8</sup>

The two series of experiments in Table IV show the influence of  $\text{H}^+$  in increasing the lability of the system. The effect is attributable specifically to  $\text{H}^+$  rather than  $\text{HSO}_4^-$ , since it decreases as  $(\text{SO}_4^{=})$  increases. The specific effect of  $\text{H}^+$  is not great (and is not expected to be great since the  $\text{H}^+$  has only a slight affinity for  $\text{SO}_4^{=}$ ), and did not appear over the variation in  $(\text{H}^+)$  executed by Adell<sup>6</sup> in dilute electrolyte solution. The differences in lability observed for solutions containing  $\text{K}^+$ ,  $\text{Na}^+$  and  $\text{Mg}^{++}$  are probably significant, and indicate increasing interaction between cation and  $\text{SO}_4^{=}$  in the order presented. The results in very acidic solution show general trends which are consistent with the ideas presented. It may be noted in addition, that the relatively slight increase in  $k_A$  from  $6.0 M \text{H}_2\text{SO}_4$  to  $9.0 M \text{H}_2\text{SO}_4$  is attributable to the decrease in activity of the water.

Comparison of the specific rates at the two temperatures leads to values of  $E$  and  $Q$  at  $0.05 M \text{SO}_4^{=}$  corresponding to  $k_A$  and  $k_S$  of  $19.3 \pm 0.5$  and  $23.7 \pm 0.5$  kcal./mole, and  $10^{10}$  and  $10^{13.5}$  l. mole<sup>-1</sup> min.<sup>-1</sup>. The change from  $\text{RH}_2\text{O}^{+++}\cdot\text{SO}_4^{=}$  to  $\text{RSO}_4^+$  has a normal frequency factor and the over-all entropy change must appear in the entropy of activation for the reverse change. This implies that the charge separation in the activated state is closer to that in  $\text{RH}_2\text{O}^{+++}\cdot\text{SO}_4^{=}$  than it is in  $\text{RSO}_4^+$ . This in turn is more in line with an activated state of coordination number 5 rather than with one of 7.<sup>4</sup>

An original purpose in undertaking the kinetic investigation of the present system was to attempt to distinguish  $\text{S}_{\text{N}}1$  and  $\text{S}_{\text{N}}2$  mechanisms on the basis that at high  $\text{SO}_4^{=}$ , a limiting rate would be expected (governed by the rate of formation of a presumed intermediate, such as  $\text{Co}(\text{NH}_3)_5^{+++}$  for the  $\text{S}_{\text{N}}1$  mechanism, whereas on the  $\text{S}_{\text{N}}2$  mechanism, such a limiting rate would not be expected. The effort to make such a distinction on kinetic evidence is vitiated however by the association of  $\text{RH}_2\text{O}^{+++}$  and  $\text{SO}_4^{=}$  which, in effect, changes the nature of the reactants. However, in view of the demonstrated effect of  $\text{SO}_4^{=}$  in increasing lability of the system, the observation that the rate of water exchange is diminished when it occurs in the presence of the net change to  $\text{RSO}_4^+$  becomes stronger evidence for an important contribution by the  $\text{S}_{\text{N}}1$  mechanism.<sup>4</sup>

Various comparisons which can be made makes it seem likely that the observations recorded here on

(7) F. J. Garrick, *Trans. Faraday Soc.*, **34**, 1088 (1939).

(8) R. A. Phoebe and H. Taube, *J. Phys. Chem.*, **56**, 33 (1952).

the equilibrium between inner sphere and outer sphere complex ions will find their counterpart in labile systems of the same charge type, as for example  $\text{Fe}^{+++}\text{-SO}_4^-$  and  $\text{Ce}^{+++}\text{-SO}_4^-$ . In general the equilibrium behavior of  $\text{Co}(\text{NH}_3)_5\text{H}_2\text{O}^{+++}$  in association reactions with anions is very nearly the same as for other tripositive ions forming 1:1 complexes. Thus, the equilibrium constant for association with  $\text{Cl}^-$  at 25° and  $\mu = 0.05$  is 4.1<sup>9</sup> and the association reaction is slightly endothermic. This behavior is in striking similarity to that of  $\text{Fe}^{+++}\text{-Cl}^-$ .<sup>10</sup> Furthermore, for  $\text{Co}(\text{NH}_3)_5^{+++}$  the affinities decrease in order from  $\text{Cl}^-$  to  $\text{I}^-$ , as they do for  $\text{Fe}^{+++}$ . The association constant observed<sup>11</sup> for  $\text{La}^{+++}$  and  $\text{SO}_4^-$  at  $\mu = 1.00$  and 25° is 25 and for  $\text{Ce}^{+++}$  and  $\text{SO}_4^-$  under the same conditions is

(9) F. J. Garrick, *Trans. Faraday Soc.*, **33**, 486 (1937).

(10) E. Rabinowitch and W. H. Stockmayer, *THIS JOURNAL*, **64**, 335 (1942).

(11) K. L. Mattern, Thesis, University of California, Berkeley, 1951.

17.5.<sup>12</sup> In the present system in the same salt environment (but at 31.1°) the constant for association involving outer sphere complexes is only 16, and if the inner sphere complexes are included, the constant would be roughly doubled. These similarities strengthen the view that for the labile systems consisting of  $\text{SO}_4^-$  and tripositive ion, the ratio of concentrations of inner and outer sphere forms will also be of the order of magnitude of unity.

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(12) T. W. Newton, private communication.

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## Low Temperature Heat Capacities of Inorganic Solids. XIV. Heat Capacity of Sodium Borohydride from 15–300°K.<sup>1</sup>

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The heat capacity of sodium borohydride has been measured from 15 to 300°K. and the thermodynamic functions have been calculated. A second-order transition, with an entropy of 1.22 e.u. occurs at 189.9°K. The entropy at 298.16 is 24.26 e.u.

### Introduction

The first low-temperature heat capacity data for sodium borohydride were obtained by Boodman, Stegeman and Mason<sup>2</sup> for the temperature range 55–298°K.

During the present investigation, the heat capacities and thermodynamic functions have been measured in the range 15–300°K., in order to extend the earlier measurements.

### Apparatus

The heat capacity measurements were made in calorimeter No. 7, one of a group of seven calorimeters for the measurement of the heat capacity of solid materials. This calorimeter is identical in all respects to calorimeter No. 1 which has been described in an earlier paper.<sup>3</sup>

The sample of sodium borohydride was obtained through the courtesy of the General Electric Research Laboratory at a reported purity of approximately 87%. The sample was purified and analyzed by the method of Davis, Mason and Stegeman<sup>4</sup> resulting in a purity of 99.60%. All handling of the sample, including filling, sealing and emptying the calorimeter was done under anhydrous conditions in a dry-box. The calorimeter contained 26.0530 g. (0.68835 mole) of sodium borohydride.

(1) This work was supported in part by the Office of Naval Research under contract with The Ohio State University Research Foundation.

(2) D. Boodman, G. Stegeman and L. Mason, Thermal Properties of some Hydrides, Univ. of Pitts., ONR Contract Number N6 ori 43, T.O.I. Technical Report, Oct. 10, 1949.

(3) H. L. Johnston and E. C. Kerr, *THIS JOURNAL*, **72**, 4733 (1950).

(4) W. D. Davis, L. S. Mason and G. Stegeman, *ibid.*, **71**, 2775 (1949).

### Experimental Results

The heat capacity data, as shown in Table I and in Fig. 1, follow a normal curve from 15°K. to about 169°K. at which point a second-order type transition occurs and the apparent heat capacity rises from about 16 calories/mole/degree to over 100 calories/mole/degree. From 193.5°K. to room temperature the heat capacity again follows a normal curve.

Below 30°K. the heat capacities followed the  $T^3$  law so that it was possible to evaluate the region below 15°K. using the equation

$$C_v = 4.90 \times 10^{-5} T^3$$

Three determinations were made to obtain an accurate value for the heat of transition. The average value obtained (see Table II) is 635.3 calories per mole for the total enthalpy change from 169–193.5°K., which corresponds to an entropy change of 3.35 e.u. By subtracting the area between 169–193.5°K. under the extrapolated portion of the normal capacity curve (Fig. 1) a value of 232.6 calories/mole was obtained for the heat of transition and a corresponding value of 1.22 e.u. for the transition entropy increase. This value is 0.22 e.u. higher than the value of 0.99 e.u. given by Boodman, Stegeman and Mason.<sup>2</sup> This is understandable, however, since their heat of transition was evaluated by a method used by Giauque and Wiebe.<sup>5</sup> The boundaries of transition were arbitrarily set as those points where the heat capacity became 0.500 calorie/gram/degree (18.924 calories/mole/degree). Since there is an apparent "pre-heat of transition" below the 0.500 calorie/gram/degree, their results would be lower than those of this research.

The values for the entropy and enthalpy (Table III) were obtained from large scale graphs of  $C_p/T$  versus  $T$  and  $C_p$  versus  $T$ , respectively, with the aid of Simpson's rule.

(5) W. F. Giauque and R. Wiebe, *ibid.*, **50**, 2193 (1928).